(12) **United States Patent**
Xu

(10) **Patent No.:** **US 9,203,671 B2**
(45) **Date of Patent:** **Dec. 1, 2015**

(54) **3D MEMORY BASED ADDRESS GENERATOR FOR COMPUTATIONALLY EFFICIENT ARCHITECTURES**

(71) Applicant: **Altera Corporation**, San Jose, CA (US)

(72) Inventor: **Lei Xu**, High Wycombe (GB)

(73) Assignee: **Altera Corporation**, San Jose, CA (US)

(*) Notice: Subject to any disclaimer, the term of this patent is extended or adjusted under 35 U.S.C. 154(b) by 433 days.

(21) Appl. No.: **13/648,443**

(22) Filed: **Oct. 10, 2012**

(65) **Prior Publication Data**

US 2014/0101409 A1   Apr. 10, 2014

(51) **Int. Cl.**
G06F 12/06 (2006.01)
H04L 27/26 (2006.01)
G06F 17/14 (2006.01)

(52) **U.S. Cl.**
CPC *H04L 27/263* (2013.01); *G06F 17/142* (2013.01); *G06F 12/06* (2013.01); *G06F 12/0623* (2013.01)

(58) **Field of Classification Search**
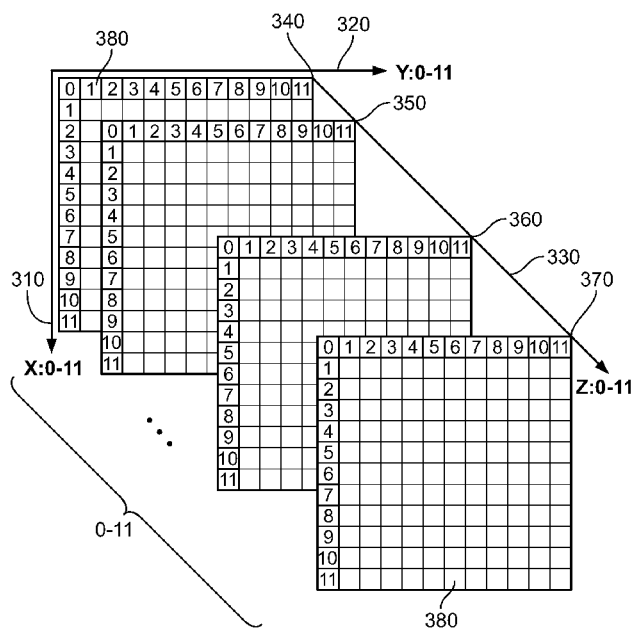CPC ... G06F 12/06; G06F 17/142; G06F 12/0623; H04L 27/263
USPC 711/217, E12.078
See application file for complete search history.

(56) **References Cited**

U.S. PATENT DOCUMENTS

6,051,179	A *	4/2000	Hagenau	264/401
6,628,819	B1 *	9/2003	Huang et al.	382/154
7,894,229	B2 *	2/2011	Lahtinen et al.	365/51
8,689,082	B2 *	4/2014	Oh et al.	714/773
2002/0006217	A1 *	1/2002	Rubbert et al.	382/131
2004/0125103	A1 *	7/2004	Kaufman et al.	345/419
2005/0062747	A1 *	3/2005	Tuomi	345/506
2006/0170672	A1 *	8/2006	Tanaka et al.	345/419
2008/0284798	A1 *	11/2008	Weybrew et al.	345/630
2008/0316501	A1 *	12/2008	Hirata et al.	356/601
2011/0309475	A1 *	12/2011	Lee	257/532
2012/0007951	A1 *	1/2012	Fogel	348/43
2013/0182483	A1 *	7/2013	Zhang	365/51
2013/0188415	A1 *	7/2013	Zhang	365/148
2014/0040592	A1 *	2/2014	Fleischer et al.	711/203

* cited by examiner

Primary Examiner — Mardochee Chery
(74) *Attorney, Agent, or Firm* — Ropes & Gray LLP

(57) **ABSTRACT**

Systems and methods are disclosed for reducing memory usage and increasing the throughput in variable-size Fast Fourier Transform (FFT) architectures. In particular, 3D symmetric virtual memory is disclosed to exploit the structure inherent in variable-size FFT computations. Data samples may be written to and read from the 3D symmetric virtual memory in a specific sequence of coordinates that exploits the structure inherent in variable-size FFT computations. Memory locations in the 3D symmetric virtual memory may be mapped to memory address in a 1D buffer using an address generation circuit.
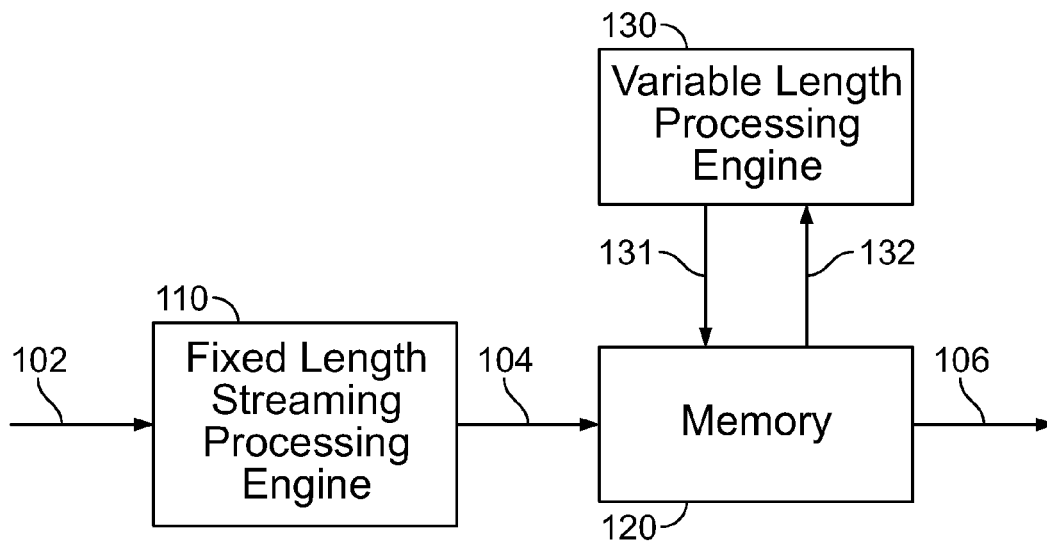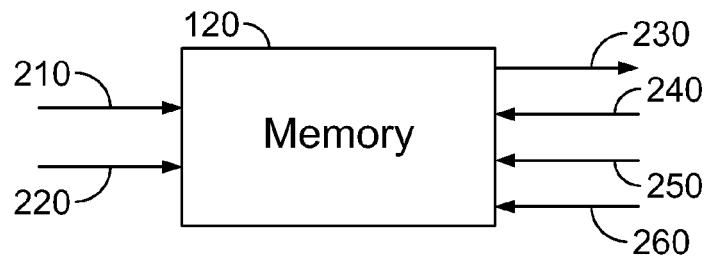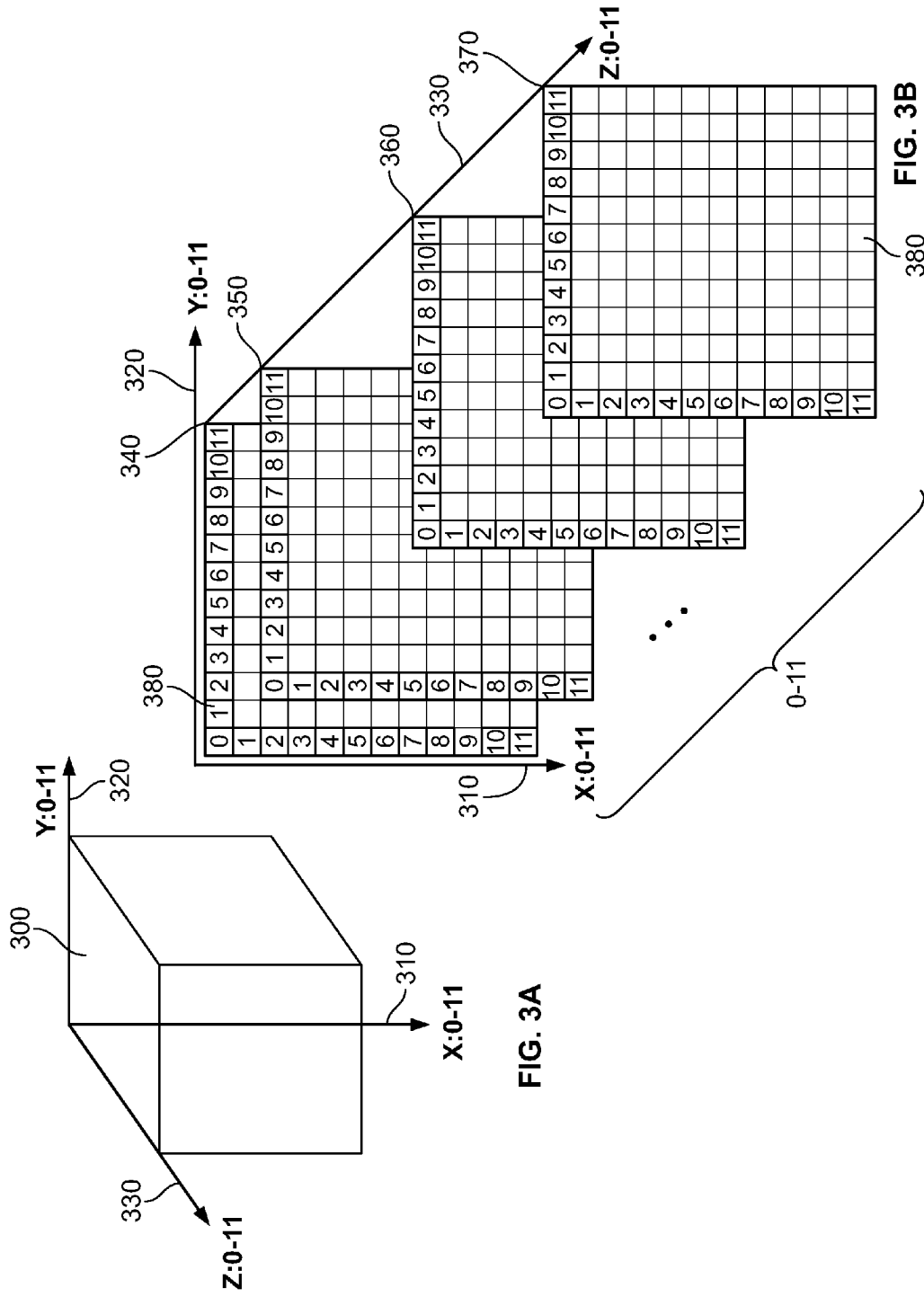
20 Claims, 11 Drawing Sheets

130

Variable Length
Processing
Engine

131

132

110

102

Fixed Length
Streaming
Processing
Engine

104

Memory

106

120

FIG. 1

120

210

Memory

220

230

240

250

260

FIG. 2

FIG. 3A

FIG. 3B

FIG. 4A

FIG. 4B

FIG. 4C

FIG. 5A

Write After Stage 1 (510, 512, 514)

Cube labels: X:0-11, Y:0-11, Z:0-11

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21
22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43
44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65
66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87
88	89	90	91	92	93	94	95	96	97	98	99	100	101	102	103	104	105	106	107	108	109
110	111	112	113	114	115	116	117	118	119	120	121	122	123	124	125	126	127	128	129	130	131
132	133	134	135	136	137	138	139	140	141	142	143	**144**	**145**	**146**	**147**	**148**	**149**	**150**	**151**	**152**	**153**
154	**155**	156	157	158	159	160	161	162	163	164	165	166	167	168	169	170	171	172	173	174	175
176	177	178	179	180	181	182	183	184	185	186	187	188	189	190	191	192	193	194	195	196	197
198	199	200	201	202	203	204	205	206	207	208	209	210	211	212	213	214	215	216	217	218	219
220	221	222	223	224	225	226	227	228	229	230	231	232	233	234	235	236	237	238	239	240	241
242	243	244	245	246	247	248	249	250	251	252	253	254	255	256	257	258	259	260	261	262	263
264	265	266	267	268	269	270	271	272	273	274	275	276	277	278	279	280	281	282	283	284	285
286	287																				

Read for Stage 2 (520, 522)

0	12	24	36	48	60	72	84	96	108	120	132	144	156	168	180	192	204	216	228	240	252
264	276	1	13	25	37	49	61	73	85	97	109	121	133	145	157	169	181	193	205	217	229
241	253	265	277	2	14	26	38	50	62	74	86	98	110	122	134	146	158	170	182	194	206
218	230	242	254	266	278	3	15	27	39	51	63	75	87	99	111	123	135	147	159	171	183
195	207	219	231	243	255	267	279	4	16	28	40	52	64	76	88	100	112	124	136	148	160
172	184	196	208	220	232	244	256	268	280	5	17	29	41	53	65	77	89	101	113	125	137
149	161	173	185	197	209	221	233	245	257	269	281	6	18	30	42	54	66	78	90	102	114
126	138	150	162	174	186	198	210	222	234	246	258	270	282	7	19	31	43	55	67	79	91
103	115	127	139	151	163	175	187	199	211	223	235	247	259	271	283	8	20	32	44	56	68
80	92	104	116	128	140	152	164	176	188	200	212	224	236	248	260	272	284	9	21	33	45
57	69	81	93	105	117	129	141	153	165	177	189	201	213	225	237	249	261	273	285	10	22
34	46	58	70	82	94	106	118	130	142	154	166	178	190	202	214	226	238	250	262	274	286
11	23	35	47	59	71	83	95	107	119	131	143	155	167	179	191	203	215	227	239	251	263
275	287																				

–   **Write After Stage 1**

530

216   532

0	12	24	36	48	60	72	84	96	108	120	132	144	156	168	180	192	204	216
228	240	252	264	276	288	300	312	324	336	348	360	372	384	396	408	420	432	
444	456	468	480	492	504	516	528	540	552	564	576	588	600	612	624	636	648	
660	672	684	696	708	720	732	744	756	768	780	792	804	816	828	840	852	864	
876	888	900	912	924	936	948	960	972	984	996	1008	1020	1032	1044	1056	1068	1080	
1092	1104	1116	1128	1140	1152	1164	1176	1188	1200	1212	1224	1236	1248	1260	1272	1284		
1296	1308	1320	1332	1344	1356	1368	1380	1392	1404	1416	1428	1440	1452	1464	1476	1488		
1500	1512	1524	1536	1548	1560	1572	1584	1596	1608	1620	1632	1644	1656	1668	1680	1692		
1704	1716																	

217   532

1	13	25	37	49	61	73	85	97	109	121	133	145	157	169	181	193	205	217
229	241	253	265	277	289	301	313	325	337	349	361	373	385	397	409	421	433	
445	457	469	481	493	505	517	529	541	553	565	577	589	601	613	625	637	649	
661	673	685	697	709	721	733	745	757	769	781	793	805	817	829	841	853	865	
877	889	901	913	925	937	949	961	973	985	997	1009	1021	1033	1045	1057	1069	1081	
1093	1105	1117	1129	1141	1153	1165	1177	1189	1201	1213	1225	1237	1249	1261	1273	1285		
1297	1309	1321	1333	1345	1357	1369	1381	1393	1405	1417	1429	1441	1453	1465	1477	1489		
1501	1513	1525	1537	1549	1561	1573	1585	1597	1609	1621	1633	1645	1657	1669	1681	1693		
1705	1717																	

218   532

2	14	26	38	50	62	74	86	98	110	122	134	146	158	170	182	194	206	218
230	242	254	266	278	290	302	314	326	338	350	362	374	386	398	410	422	434	
446	458	470	482	494	506	518	530	542	554	566	578	590	602	614	626	638	650	
662	674	686	698	710	722	734	746	758	770	782	794	806	818	830	842	854	866	
878	890	902	914	926	938	950	962	974	986	998	1010	1022	1034	1046	1058	1070		
1082	1094	1106	1118	1130	1142	1154	1166	1178	1190	1202	1214	1226	1238	1250	1262	1274		
1286	1298	1310	1322	1334	1346	1358	1370	1382	1394	1406	1418	1430	1442	1454	1466	1478		
1490	1502	1514	1526	1538	1550	1562	1574	1586	1598	1610	1622	1634	1646	1658	1670	1682		
1694	1706	1718																

Y:0-11   X:0-11

FIG. 5B

Read for Stage 2

540

542

0	144	288	432	576	720	864	1008	1152	1296	1440	1584	1	145	289	433	577	721
865	1009	1153	1297	1441	1585	2	146	290	434	578	722	866	1010	1154	1298	1442	1586
1595	12	156	300	444	588	732	876	1020	1164	1308	1452	1596	13	157	301	445	589
733	877	1021	1165	1309	1453	1597	14	158	302	446	590	734	878	1022	1166	1310	1454
1463	1607	24	168	312	456	600	744	888	1032	1176	1320	1464	1608	25	169	313	457
601	745	889	1033	1177	1321	1465	1609	26	170	314	458	602	746	890	1034	1178	1322
1331	1475	1619	36	180	324	468	612	756	900	1044	1188	1332	1476	1620	37	181	325
325	469	613	757	901	1045	1189	1333	1477	1621	38	182	326	470	614	758	902	1046
913	1057	1201	1345	1489	1633	50	194	338	482	626	770	914	1058	1202	1346	1490	1634
1643	60	204	348	492	636	780	924	1068	1212	1356	1500	1644	61	205	349	493	637
781	925	1069	1213	1357	1501	1645	62	206	350	494	638	782	926	1070	1214	1358	1502
1511	1655	72	216	360	504	648	792	936	1080	1224	1368	1512	1656	73	217	361	505
505	649	793	937	1081	1225	1369	1513	1657	74	218	362	506	650	794	938	1082	1226
1235	1379	1523	1667	84	228	372	516	660	804	948	1092	1236	1380	1524	1668	85	229
229	373	517	661	805	949	1093	1237	1381	1525	1669	86	230	374	518	662	806	950
1103	1247	1391	1535	1679	96	240	384	528	672	816	960	1104	1248	1392	1536	1680	97
97	241	385	529	673	817	961	1105	1249	1393	1537	1681	98	242	386	530	674	818
971	1115	1259	1403	1547	1691	108	252	396	540	684	828	972	1116	1260	1404	1548	1692
1692	109	253	397	541	685	829	973	1117	1261	1405	1549	1693	110	254	398	542	686
695	839	983	1127	1271	1415	1559	1703	120	264	408	552	696	840	984	1128	1272	1416
1416	1560	1704	121	265	409	553	697	841	985	1129	1273	1417	1561	1705	122	266	410
419	563	707	851	995	1139	1283	1427	1571	1715	132	276	420	564	708	852	996	1140
1140	1284	1428	1572	1716	133	277	421	565	709	853	997	1141	1285	1429	1573	1717	134
134	278	422	566	710	854	998	1142	1286	1430	1574	1718	135	279	423	567	711	855

FIG. 5B (Cont.)

Write After Stage 1 — 550

0	144	288	432	576	720	864	1008	1152	1296	1440
1584	1	145	289	433	577	721	865	1009	1153	1297
1441	1585	2	146	290	434	578	722	866	1010	1154
1298	1442	1586	3	147	291	435	579	723	867	1011
1155	1299	1443	1587	4	148	292	436	580	724	868
1012	1156	1300	1444	1588	5	149	293	437	581	725
869	1013	1157	1301	1445	1589	6	150	294	438	582
726	870	1014	1158	1302	1446	1590	7	151	295	439
583	727	871	1015	1159	1303	1447	1591	8	152	296
440	584	728	872	1016	1160	1304	1448	1592	9	153
297	441	585	729	873	1017	1161	1305	1449	1593	10
154	298	442	586	730	874	1018	1162	1306	1450	1594
11	155	299	443	587	731	875	1019	1163	1307	1451
1595										

552

Read for Stage 2 — 560

0	1	2	3	4	5	6	7	8	9	10	11
144	145	146	147	148	149	150	151	152	153	154	155
288	289	290	291	292	293	294	295	296	297	298	299
432	433	434	435	436	437	438	439	440	441	442	443
576	577	578	579	580	581	582	583	584	585	586	587
720	721	722	723	724	725	726	727	728	729	730	731
864	865	866	867	868	869	870	871	872	873	874	875
1008	1009	1010	1011	1012	1013	1014	1015	1016	1017	1018	1019
1152	1153	1154	1155	1156	1157	1158	1159	1160	1161	1162	1163
1296	1297	1298	1299	1300	1301	1302	1303	1304	1305	1306	1307
1440	1441	1442	1443	1444	1445	1446	1447	1448	1449	1450	1451
1584	1585	1586	1587	1588	1589	1590	1591	1592	1593	1594	1595

562

Y:0-11
X:0-11
Z:0-11

FIG. 5C

FIG. 6

FIG. 7

FIG. 7 (Cont.)

800

810

Peripheral
Devices

840

I/O

850

830

Integrated
Circuit

860

820

Processor

870

Memory

880

FIG. 8

3D MEMORY BASED ADDRESS GENERATOR FOR COMPUTATIONALLY EFFICIENT ARCHITECTURES

BACKGROUND OF THE DISCLOSURE

This disclosure relates to systems and methods for reducing memory usage and increasing the throughput in variable-size Fast Fourier Transform (FFT) architectures.

3GPP Long Term Evolution (LTE) is a wireless communication standard that supports high-speed wireless communications. LTE is a communication standard that is based on both Single-Carrier Frequency Division Multiplexing (SC-FDM) and Orthogonal Frequency Division Multiplexing (OFDM) algorithms that make heavy utilization of FFTs like the variable-size Discrete Fourier Transform (DFT) or the Inverse Discrete Fourier Transform (IDFT).

An FFT calculation includes reading an input data sequence with data samples $x[n]$, $n=0, \ldots, N-1$, where N is the length of the input data sequence, and outputting the frequency domain FFT data sequence with data samples $X[k]$, $k=0, \ldots, N-1$. Such a calculation is conventionally called an N-point FFT. FFT algorithms use a divide and conquer approach to reduce the computational complexity of calculating an FFT. For example, the Cooley-Tukey algorithm recursively decomposes the problem of calculating the FFT into two sub-problems of half the size (i.e., N/2) at every intermediate pass. The size of the FFT decomposition is known as the radix. In the above example, the radix is 2. This decomposition approach generally works for any radix k provided that N is a power of k. Thus, calculating an FFT typically involves making a number of passes (also referred to as stages) over the input data sequence and intermediate results. In general, each pass can be associated with a different radix.

The LTE standard commonly uses FFT algorithms with radix R=2, 3, 4, or 5. As an example, consider the calculation of a 64-point FFT using the radix R=4. For computing the FFT, an FFT processor conventionally processes the input data sequence in the order where the indices corresponding to the data samples are arranged in the following order:
00, 16, 32, 48, 01, 17, 33, 49, 02, 18, 34, 50, 03, 19, 35, 51, 04, 20, 36, 52, \ldots, 15, 31, 47, 63.
This order of data samples is referred to as a radix-reversed order. In the first pass of the FFT calculation, data samples corresponding to indices 00, 16, 32, and 48 are used to compute a first radix-4 butterfly; data samples corresponding to indices 01, 17, 33, and 49 are used to compute the next radix-4 butterfly; and so on. An FFT butterfly is a portion of the FFT calculation that breaks up the larger FFT calculation into smaller sub-transform calculations.

It has been noted that variable-size DFT/IDFT implementations often require high memory usage and suffer from low throughput. Accordingly, it is beneficial to have architectures capable of performing DFT/IDFT computations efficiently. If efficient architectures for performing such computations are not available, DFT/IDFT computations may become a bottleneck preventing LTE based communication schemes from operating optimally.

Some current variable-size DFT/IDFT implementations utilize dual processing cores in order to meet LTE throughput requirements. Some current variable-size DFT/IDFT implementations additionally utilize double dual port memory to meet the memory usage requirements. For example, some variable-size DFT/IDFT implementations utilize a ping-pong buffer which includes two separate storage arrays arranged in a configuration that allows reading and writing of data to

occur in parallel. In particular, each storage array may have an independent data bus that may, in a first time period, enable data to be written to the first storage array while data is being read from the second storage array. In a second time period, data may be read from the first storage array while data is written to the second storage array. In subsequent time periods, the reading and writing of data to each storage array may alternate in the manner described above.

However, utilizing a ping-pong buffer comes with the cost of increased memory requirements, i.e., more memory is required than if a single storage array was utilized. Therefore, it would be desirable to have methods and systems for performing variable-size FFTs efficiently without increasing memory requirements.

SUMMARY OF THE DISCLOSURE

To address the above and other shortcomings within the art, the present disclosure provides methods and systems for reducing memory usage and increasing the throughput in variable-size Fast Fourier Transform (FFT) architectures.

In an embodiment, the system includes a buffer operable to store data samples that may be operated upon to compute an FFT. Memory locations in the buffer may be mapped to a 3D symmetric virtual memory operable to exploit the structure inherent in variable-length FFT computations. The system may include address generator circuitry operable to map memory locations in the 3D symmetric virtual memory to the buffer.

In an embodiment, the system may include a fixed-length streaming processing engine operable to compute fixed-length FFTs, a variable-length processing engine operable to compute variable-length FFTs, and the buffer for storing initial, intermediate, and/or final results of the FFT computations. The buffer may be abstracted as a 3D symmetric virtual memory.

In an embodiment, data samples may be written to and read from the 3D symmetric virtual memory in a specific coordinate sequence. For example, data samples may initially be written to the 3D symmetric virtual memory first along the Y coordinate, followed by the X and Z coordinates respectively. Data samples may then be read from the 3D symmetric virtual memory in the same coordinate sequence. In addition, as particular memory slices of the 3D symmetric virtual memory are released, i.e., data samples are read from them, other data samples may be written to the released memory slices. The coordinate sequence in which data samples may be written to the 3D symmetric virtual memory may be first along the X coordinate, followed by the Z and Y coordinates respectively. Data samples may then be read from the 3D symmetric virtual memory in the same coordinate sequence.

Next, data samples may be written to the 3D symmetric virtual memory first along the Z coordinate, followed by the Y and X coordinates respectively. Data samples may then be read from the 3D symmetric virtual memory in the same coordinate sequence. The order in which data samples are written to and read from the 3D symmetric virtual memory may then be repeated starting from the coordinate sequence where data samples are first written along the Y coordinate, followed by the X and Z coordinates respectively.

In an embodiment, an address generator circuit may be operable to convert indices of memory locations in the 3D symmetric virtual memory to memory addresses in the buffer. The address generator circuit may include cyclic counters and additional circuitry operable to assist in the conversion of memory locations in the 3D symmetric virtual memory to memory addresses in the buffer. The address generator circuit

may be dynamically reconfigurable under the control of a state machine to compute memory addresses in the buffer based on the coordinate sequence in which data samples are being read from or written to the 3D symmetric virtual memory.

BRIEF DESCRIPTION OF THE DRAWINGS

Further features of the disclosure, its nature and various advantages will be apparent upon consideration of the following detailed description, taken in conjunction with the accompanying drawings, in which like reference characters refer to like parts throughout, and in which:

FIG. 1 is a simplified block diagram of an efficient FFT computation architecture, according to an illustrative embodiment;

FIG. 2 is a simplified block diagram of a dual port memory, according to an illustrative embodiment;

FIGS. 3A and 3B are simplified block diagrams of a 3D memory, according to an illustrative embodiment;

FIGS. 4A, 4B, and 4C are simplified block diagrams showing the manner in which data may be read from and written to a 3D memory, according to an illustrative embodiment;

FIGS. 5A, 5B, and 5C are simplified tables showing the manner in which data may be read from and written to a 3D memory, according to an illustrative embodiment;

FIG. 6 is a simplified block diagram of an addressor circuit that may be used to generate addresses for the buffer, according to an illustrative embodiment;

FIG. 7 is a simplified block diagram of an addressor circuit that may be used to generate addresses for the buffer using backpressure, according to an illustrative embodiment; and

FIG. 8 illustrates a circuit or other device that includes embodiments of the circuits described herein as being within a data processing system.

DETAILED DESCRIPTION OF THE INVENTION

To provide an overall understanding of the invention, certain illustrative embodiments will now be described. However, it will be understood by one of ordinary skill in the art that the systems and methods described herein may be adapted and modified as is appropriate for the application being addressed and that the systems and methods described herein may be employed in other suitable applications, and that such other additions and modifications will not depart from the scope hereof.

FIG. 1 is a simplified block diagram of an efficient FFT computation architecture, according to an illustrative embodiment. In some embodiments, at least some components of the FFT computation architecture may be located on an integrated circuit, an application-specific integrated circuit (ASIC), an application-specific standard product (ASSP), a Programmable Logic Device (PLD), a Field Programmable Gate Array (FPGA), a full-custom chip, or a dedicated chip. It should also be understood that the FFT computation architecture may be located on a combination of devices, such as a FPGA and an ASIC, and/or may include additional, standalone circuit components.

The FFT computation architecture may include fixed length streaming processing engine 110, memory 120, and variable length processing engine 130. Fixed length streaming processing engine 110 may be operative to receive a streaming input in a symbol-reversed order via bus 102. Fixed length streaming processing engine 110 may be connected to memory 120 via line 104. Memory 120 may be connected to variable length processing engine 120 via buses 131 and 132. Memory

120 may be operative to output data via bus 106. Memory 120 is described in greater detail below in connection with FIG. 2.

Fixed length streaming processing engine 110 may be circuitry operative to perform fixed length FFT computations which have a constant size of points for the data frames whose FFT is being calculated. Fixed length streaming processing engine 110 may include multiple butterfly circuits and shift registers (not shown). In some implementations, fixed length streaming processing engine 110 may store intermediate computation values and/or results of the fixed length FFT computation in memory 120 using bus 104.

Variable length processing engine 130 may be circuitry operative to perform variable length FFT computations where the size of different frames for the FFT calculation is variable (normally a multiple of an element of a common radix set). In some implementations, there may be multiple variable length processing engines (not shown) operating in parallel. Variable length processing engine 130 may store intermediate computation values and/or results of the variable length FFT computation in memory 120 using buses 131 and 132. In some implementations, fixed length streaming processing engine 110 and variable length processing engine 130 may be capable of operating at different clock frequencies.

FIG. 2 is a simplified block diagram of a dual port memory, according to an illustrative embodiment. In some implementations, memory 120 may be a 1D storage array. Memory 120 may be operative to receive data from fixed length streaming processing engine 110 via buses 210 and 220. Buses 210 and 220 may be part of bus 104 of FIG. 1. Bus 210 may be operative to transmit to memory 120, from fixed length streaming processing engine 110, addresses of memory locations that fixed length streaming processing engine 110 desires to write data to. Bus 220 may be operative to transmit to memory 120, from fixed length streaming processing engine 110, data that fixed length streaming processing engine 110 desires to write to memory 120.

Memory 120 may be connected to variable length processing engine 130 via buses 230, 240, 250, and 260. Buses 230 and 240, and buses 250 and 260, may respectively be part of buses 131 and 132 of FIG. 1. Buses 230 and 240 may be used by variable length processing engine 130 to read data from memory 120. More specifically, bus 240 may be operative to transmit to memory 120, from variable length processing engine 130, addresses of memory locations that variable length processing engine 130 desires to read data from. Bus 230 may be operative to transmit data from the memory locations specified by variable length processing engine 130 via bus 240 to variable length processing engine 130.

Buses 250 and 260 may be used by variable length processing engine 130 to write data to memory 120. More specifically, bus 250 may be operative to transmit to memory 120, from variable length processing engine 130, addresses of memory locations that variable length processing engine 130 desires to write data to. Bus 260 may be operative to transmit to memory 120, from variable length processing engine 130, data that variable length processing engine 130 desires to write to memory 120.

As discussed above, buses 230, 240, 250, and 260 may provide variable length processing engine 130 the ability to read and write data from memory 120 simultaneously. In some implementations, memory 120 may use reduced ports for reading and writing data and may be shared with external logic. For example, memory 120 may utilize single ports in combination with external logic. In some implementations, a ready/busy signal (not shown) may be used to acknowledge a module located before or after memory 120 to determine

whether to continue reading or writing data from memory **120** or to temporarily pause reading or writing data from memory **120**.

FIGS. **3A** and **3B** are simplified block diagrams of a 3D memory, according to an illustrative embodiment. In particular, memory **120** of FIG. **1** and FIG. **2** may be abstractly represented as a 3D memory of the form shown in FIGS. **3A** and **3B**. FIG. **3A** shows an exemplary embodiment in which memory **120** of FIG. **1** may be represented as a 3D cube **300**. Cube **300** may be symmetric. The three axes of cube **300** may be indicated by axes X **310**, Y **320**, and Z **330**. Cube **300** may merely be an abstract representation of memory **120**, i.e., memory **120** may not be structured as cube **300** in architectural implementations.

FIG. **3B** shows a cross-sectional view of cube **300** of FIG. **3A** illustrating a manner in which the internal structure of cube **300** may be configured. FIG. **3B** shows a representation of cube **300** cross-sectioned along axis X **310**. For example, cube **300** may include cross-section slices **340**, **350**, **360**, and **370**. Cross-section slices **340**, **350**, **360**, and **370** may each be a planar memory structure containing memory locations **380**. Slices **340**, **350**, **360**, and **370** may be stacked next to each other in some implementations. Cube **300** may include additional slices (not shown) similar to slices **340**, **350**, **360**, and **370**. Each memory location **380** may be capable of storing a data sample. In some implementations, each data sample may be a sub-carrier sample.

FIG. **3B** shows that in some implementations, each slice **340**, **350**, **360**, and **370** may be able to store 12×12 data samples. For example, memory locations in each slice **340**, **350**, **360**, and **370** may be indexed from 0:11 in each dimension as shown in FIG. **3B**. Accordingly, memory locations in cube **300** may be indexed using vector coordinate notation for ease of representation. For example, the memory location at coordinates (X=0, Y=0, Z=0) may be denoted by the notation (0,0,0). For example, the memory location at coordinates (X=0, Y=11, Z=0) may be denoted by the notation (0,11,0). A sequence of memory locations in cube **300** may accordingly be denoted by using the above notation. For example, a sequence of memory locations along column **390** of slice **340** may be denoted by (0,0,0), (1,0,0), (2,0,0), . . . (11,0,0) or equivalently by [X=0:11, Y=0, Z=0]. For example, a sequence of memory locations along the first row of slice **340** may be denoted by (0,0,0), (0,1,0), (0,2,0), . . . (0,11,0) or equivalently by [X=0, Y=0:11, Z=0].

Because cube **300** is a representation of memory **120**, each memory location in cube **300** may correspond to a memory address in memory **120**. For example, memory location (0,0, 0) may correspond to a particular memory address in memory **120**. The size of slices **340**, **350**, **360**, and **370** shown in FIG. **3B** is merely illustrative and memory slices capable of storing additional or fewer data samples may be utilized in some implementations.

FIGS. **4A**, **4B**, and **4C** are simplified block diagrams showing the manner in which data may be read from and written to a 3D memory, according to an illustrative embodiment. FIG. **4A** shows cube **400** which is a representation of memory **120** of FIG. **1**. Cube **400** may be substantially identical to cube **300** of FIG. **3A**. The three axes of cube **400** may be indicated by axes X **410**, Y **420**, and Z **430**. As an example, FIGS. **4A**, **4B**, and **4C** show how data may be read from and written to cube **400** when variable length processing engine **130** uses radix R=12 during FFT computations. Radix R=12 is used frequently during FFT computations required in the LTE standard. However, other values of the radix may also be used.

FIG. **4A** shows that variable length processing engine **130** may initially write data to memory block **440**. Memory block **440** may correspond to the set of memory locations denoted by:

$$[X = 0, \quad Y = 0:11, \quad Z = 0], \tag{1}$$
$$[X = 1, \quad Y = 0:11, \quad Z = 0],$$
$$\vdots$$
$$[X = 11, \quad Y = 0:11, \quad Z = 0].$$

Memory block **440** may be substantially similar to slice **340** of FIG. **3B**. Moreover, equation (1) may indicate the order in which data are written to memory locations in memory block **440**. For example, the first data sample may be written to memory location (0,0,0), the second data sample may be written to memory location (0,1,0), and the twelfth data sample may be written to memory location (0,11,0). In other words, the first twelve data samples may be written to memory locations [X=0, Y=0:11, Z=0]. The next twelve data samples may be written to memory locations [X=1, Y=0:11, Z=0], starting from memory location (1, 0, 0), and so on. Data samples **132** to **144** may be written to memory locations [X=11, Y=0:11, Z=0].

Subsequently, in a manner similar to that described above in connection with memory block **440**, data may be written to a memory block that corresponds to slice **350** of FIG. **3B**, as indicated below by the memory locations denoted by:

$$[X = 0, \quad Y = 0:11, \quad Z = 1], \tag{2}$$
$$[X = 1, \quad Y = 0:11, \quad Z = 1],$$
$$\vdots$$
$$[X = 11, \quad Y = 0:11, \quad Z = 1].$$

Subsequently, data may be written to memory locations denoted by: [X=0, Y=0:11, Z=2], [X=0, Y=0:11, Z=2], . . . , [X=0, Y=0:11, Z=2], and so on. Proceeding in this manner, data may eventually be written to memory locations denoted by:

$$[X = 0, \quad Y = 0:11, \quad Z = 11], \tag{3}$$
$$[X = 1, \quad Y = 0:11, \quad Z = 11],$$
$$\vdots$$
$$[X = 11, \quad Y = 0:11, \quad Z = 11].$$

Equations (1)-(3) indicate the order in which data may be written to memory locations in cube **400**. It may not necessarily be that all memory locations in cube **400** are filled with data because variable length processing engine **130** which writes data to memory **120** (represented by cube **400**) may be computing a variable length FFT. The data written to memory locations denoted by equations (1)-(3) may correspond to sub-carrier samples whose IDFT may need to be computed. Writing data to cube **400** in the order specified by equations (1)-(3) is represented by the notation Y-X-Z, i.e., the data is first written along axis Y **420**, followed by axis X **410**, and lastly data is written along axis Z **430**.

FIG. 4B shows an illustrative example of the manner in which data may be read from cube **400**. Reading of data in this manner may correspond to reading data for performing computations for a second stage of an IDFT being computed by variable length processing engine **130**.

FIG. 4B shows that variable length processing engine **130** may initially read data from memory block **450**. Memory block **450** may correspond to the set of memory locations denoted by:

$$[X = 0\!:\!11, \quad Y = 0, \quad Z = 0], \tag{4}$$
$$[X = 0\!:\!11, \quad Y = 0, \quad Z = 1],$$
$$\vdots$$
$$[X = 0\!:\!11, \quad Y = 0, \quad Z = 11].$$

Equation (4) may indicate the order in which data are read from memory locations in memory block **450**. For example, the first data sample may be read from memory location (0,0,0), the second data sample may be read from memory location (1,0,0), and the twelfth data sample may be read from memory location (11,0,0). In other words, the first twelve data samples may be read from memory locations [X=0:11, Y=0, Z=0]. The next twelve data samples may be read from memory locations [X=0:11, Y=0, Z=1], starting from memory location (0, 0, 1), and so on. Data samples **132** to **144** may be read from memory locations [X=0:11, Y=0, Z=11].

Subsequently, data may be read from memory locations denoted by:

$$[X = 0\!:\!11, \quad Y = 1, \quad Z = 0], \tag{5}$$
$$[X = 0\!:\!11, \quad Y = 1, \quad Z = 1],$$
$$\vdots$$
$$[X = 0\!:\!11, \quad Y = 1, \quad Z = 11].$$

Still further, data may be read from memory locations denoted by:

$$[X = 0\!:\!11, \quad Y = 11, \quad Z = 0], \tag{6}$$
$$[X = 0\!:\!11, \quad Y = 11, \quad Z = 1],$$
$$\vdots$$
$$[X = 0\!:\!11, \quad Y = 11, \quad Z = 11].$$

Reading data from cube **400** in the order specified by equations (4)-(6) is represented by the notation X-Z-Y, i.e., the data is first read along axis X **410**, followed by axis Z **430**, and lastly data is read along axis Y **420**.

Once data has been read from memory block **450**, memory block **450** may be released or freed up, i.e., memory locations in memory block **450** may be used for storing other data. The process by which memory block (or slices) are released is described further in connection with FIG. **7** below.

In particular, as explained in greater detail in connection with FIGS. **5A**, **5B**, and **5C** below, once memory locations in memory block **450** are released, they may be used for storing other data. Specifically, the order in which memory locations of cube **400** are used to store data may be identical to the order in which data is read from memory locations in cube **400** as

described in connection with FIG. **4B**. For example, data may be written to cube **400** in the order X-Z-Y, i.e., the data is first written along axis X **410**, followed by axis Z **430**, and lastly data is written along axis Y **420**.

In other words, data may be written to the set of memory locations denoted by:

$$[X = 0\!:\!11, \quad Y = 0, \quad Z = 0], \tag{7}$$
$$[X = 0\!:\!11, \quad Y = 0, \quad Z = 1],$$
$$\vdots$$
$$[X = 0\!:\!11, \quad Y = 0, \quad Z = 11].$$

For example, the first data sample may be written to memory location (0,0,0), the second data sample may be written to memory location (1,0,0), and the twelfth data sample may be written to memory location (11,0,0). In other words, the first 12 data samples may be written to memory locations [X=0: 11, Y=0, Z=0]. The next twelve data samples may be written to memory locations [X=0:11, Y=0, Z=1], starting from memory location (0, 0, 1), and so on. Data samples **132** to **144** may be written to memory locations [X=0:11, Y=0, Z=11].

Subsequently, data may be written to memory locations denoted by:

$$[X = 0\!:\!11, \quad Y = 1, \quad Z = 0], \tag{8}$$
$$[X = 0\!:\!11, \quad Y = 1, \quad Z = 1],$$
$$\vdots$$
$$[X = 0\!:\!11, \quad Y = 1, \quad Z = 11].$$

Still further, data may be written to memory locations denoted by:

$$[X = 0\!:\!11, \quad Y = 11, \quad Z = 0], \tag{9}$$
$$[X = 0\!:\!11, \quad Y = 11, \quad Z = 1],$$
$$\vdots$$
$$[X = 0\!:\!11, \quad Y = 11, \quad Z = 11].$$

FIG. 4C shows an illustrative example of the manner in which data may be read from cube **400**. Reading of data in this manner may correspond to reading data for performing computations for a third stage of an IDFT being computed by variable length processing engine **130**.

FIG. 4C shows that variable length processing engine **130** may initially read data from memory block **460**. Memory block **460** may correspond to the set of memory locations denoted by:

$$[X = 0, \quad Y = 0, \quad Z = 0\!:\!11], \tag{10}$$
$$[X = 0, \quad Y = 1, \quad Z = 0\!:\!11],$$
$$\vdots$$
$$[X = 0, \quad Y = 11, \quad Z = 0\!:\!11].$$

Equation (10) may indicate the order in which data are read from memory locations in memory block **460**. For example,

the first data sample may be read from memory location (0,0,0), the second data sample may be read from memory location (0,0,1), and the twelfth data sample may be read from memory location (0,0,11). In other words, the first 12 data samples may be read from memory locations [X=0, Y=0, Z=0:11]. The next twelve data samples may be read from memory locations [X=0, Y=1, Z=0:11], starting from memory location (0, 1, 0), and so on. Data samples **132** to **144** may be read from memory locations [X=0, Y=11, Z=0:11].

Subsequently, data may be read from memory locations denoted by:

$$[X = 1, \quad Y = 0, \quad Z = 0:11], \tag{11}$$
$$[X = 1, \quad Y = 1, \quad Z = 0:11],$$
$$\vdots$$
$$[X = 1, \quad Y = 11, \quad Z = 0:11].$$

Still further, data may be read from memory locations denoted by:

$$[X = 11, \quad Y = 0, \quad Z = 0:11], \tag{12}$$
$$[X = 11, \quad Y = 1, \quad Z = 0:11],$$
$$\vdots$$
$$[X = 11, \quad Y = 11, \quad Z = 0:11].$$

Reading data from cube **400** in the order specified by equations (10)-(12) is represented by the notation Z-Y-X, i.e., the data is first read along axis Z **430**, followed by axis Y **420**, and lastly data is read along axis X **410**.

Once memory locations in memory block **460** are released, they may be used for storing other data. Specifically, the order in which memory locations of cube **400** are used to store data may be identical to the order in which data is read from memory locations in cube **400** as described in connection with FIG. **4C**. For example, data may be written to cube **400** in the order Z-Y-X, i.e., the data is first written along axis Z **430**, followed by axis Y **420**, and lastly data is written along axis X **410**.

Subsequently, data may be read from memory block **440** as shown in FIG. **4A** in the order specified Y-X-Z, i.e., the data is first read along axis Y **420**, followed by axis X **410**, and lastly data is read along axis Z **430**. Memory block **440** may correspond to the set of memory locations denoted by:

$$[X = 0, \quad Y = 0:11, \quad Z = 0],$$
$$[X = 1, \quad Y = 0:11, \quad Z = 0],$$
$$\vdots$$
$$[X = 11, \quad Y = 0:11, \quad Z = 0].$$

The process of reading and writing data to cube **400**, as discussed above in connection with FIGS. **4A**, **4B**, and **4C** is further elaborated below in FIGS. **5A**, **5B**, and **5C** by means of an example.

FIGS. **5A**, **5B**, and **5C** are simplified tables showing the manner in which data may be read from and written to a 3D memory, according to an illustrative embodiment. As an example, FIGS. **5A**, **5B**, and **5C** show how data may be read

from and written to cube **400** of FIG. **4A** when variable length processing engine **130** uses radix R=12 during FFT computations. Other values of the radix may also be used.

FIG. **5A** shows tables **510** and **520** of indices of data samples. In an illustrative example, variable length processing engine **130** may be computing a variable length FFT where the frame length of an initial data frame may be 12×24=288 data samples. In a first stage, variable length processing engine **130** may write data samples corresponding to the initial frame to memory **120**. Table **510** lists indices of data samples in the sequence in which the data samples may be stored in cube **400** of FIG. **4A** which is a representation of memory **120**. Mapping of memory locations in cube **400** to memory locations in memory **120**, and the subsequent generation of addresses corresponding to memory locations in memory **120** is described below in connection with FIGS. **6** and **7**.

Table **510** lists indices of data samples in the sequence in which the data samples may be stored in cube **400** of FIG. **4A**. In particular, variable length processing engine **130** may write data samples to cube **400** in the same sequence as specified in connection with FIG. **4A**. Specifically, variable length processing engine **130** may write the first data sample memory location (0,0,0), the second data sample to memory location (0,1,0), and the twelfth data sample to memory location (0,11, 0). In other words, the first twelve data samples, indicated in table **510** as data samples **512**, may be written to memory locations [X=0, Y=0:11, Z=0]. The next twelve data samples may be written to memory locations [X=1, Y=0:11, Z=0], starting from memory location (1, 0, 0), and so on. Data samples **132** to **144** may be written to memory locations [X=11, Y=0:11, Z=0]. This order is represented by: [X=0, Y=0:11, Z=0], [X=1, Y=0:11, Z=0], . . . , [X=11, Y=0:11, Z=0].

Subsequently, data may be written to memory locations denoted by: [X=0, Y=0:11, Z=1], [X=1, Y=0:11, Z=1], . . . , [X=11, Y=0:11, Z=1], followed by the memory locations denoted by: [X=0, Y=0:11, Z=2], [X=0, Y=0:11, Z=2], . . . , [X=0, Y=0:11, Z=2], and so on. Writing data to cube **400** in the order specified above is represented by the notation Y-X-Z, i.e., the data is first written along axis Y **420**, followed by axis X **410**, and lastly data is written along axis Z **430**.

In a second stage of the FFT computation, variable length processing engine **130** may read data samples corresponding to the initial frame from memory **120**. Table **520** lists indices of data samples in the sequence in which the data samples may be read from cube **400** of FIG. **4A**. In particular, variable length processing engine **130** may read data samples to cube **400** in the same sequence as specified in connection with FIG. **4B**.

Specifically, variable length processing engine **130** may read a first data sample from memory location (0,0,0), the second data sample may be read from memory location (1,0, 0), and the twelfth data sample may be read from memory location (11,0,0). In other words, the first twelve data samples may be read from memory locations [X=0:11, Y=0, Z=0]. Furthermore, as shown in table **520**, reading data samples from cube **400** in this sequence corresponds to reading data samples with indices are 0, 12, 24, 36, 48, 60, 72, 84, 96, 108, 120, and 132. This sequence of indices of data samples is referred to as the radix-reversed sequence in literature and is the sequence in which the data samples may be processed by variable length processing engine **130** during the second stage of the FFT computation. Accordingly, it is advantageous that the sequence of memory locations of cube **400** from which

data samples are read may result in reading data samples in the order in which they may be processed by variable length processing engine 130.

The next twelve data samples may be read from memory locations [X=0:11, Y=0, Z=1], starting from memory location (0, 0, 1), and so on. Subsequently, data may be read from memory locations denoted by: [X=0:11, Y=1, Z=0], [X=0:11, Y=1, Z=1], . . . , [X=0:11, Y=1, Z=11]. Still further, data may be read from memory locations denoted by: [X=0:11, Y=11, Z=0], [X=0:11, Y=11, Z=1], . . . , [X=0:11, Y=11, Z=11]. Reading data from cube 400 in the order specified above is represented by the notation X-Z-Y, i.e., the data is first read along axis X 410, followed by axis Z 430, and lastly data is read along axis Y 420.

Variable length processing engine 130 may read data samples from cube 400 in the sequence specified above until variable length processing engine 130 has read the data sample with index 278. The sequence of data samples with indices 0, 12, 24, . . . , 254, 266, 278 is denoted by sequence 522 in table 520. Once the data samples in sequence 522 have been read by variable length processing engine 130, the memory locations in which the read data samples were stored may be released. The released memory locations may then be utilized by cube 400 for storage of other data as described below in connection with FIG. 5B.

Continuing the previous example, variable length processing engine 130 may be computing a variable length FFT where the frame length of an initial data frame may be 12×36=432 data samples. In a first stage, variable length processing engine 130 may write data samples corresponding to the initial frame to memory 120.

FIG. 5B shows tables 530 and 540 of indices of data samples. Table 530 lists indices of data samples in the sequence in which the data samples may be stored in cube 400 of FIG. 4A. The order in which memory locations of cube 400 are used to store data may be identical to the order in which data is read from memory locations in cube 400 as described in connection with table 520 of FIG. 5A. For example, data may be written to cube 400 in the order X-Z-Y, i.e., the data is first written along axis X 410, followed by axis Z 430, and lastly data is written along axis Y 420. After the completion of these three write phases, the state of the memory (i.e., cube 400) returns to the first stage described above in connection with FIG. 5A.

FIG. 6 is a simplified block diagram of an addressor circuit that may be used to generate addresses for the buffer, according to an illustrative embodiment. System 600 includes adders 620 and 630, counters 642, 644, and 646, switch 610, and shift registers 652, 654, 656, and 658. Lead 602 may output a memory address to buses 210, 230 or 250 of FIG. 2. In some implementations, clock 612 may be an external 33 MHz clock signal, although clock 612 may also be a clock signal running at other frequencies. Clock 612 may be operable to clock all the components of system 600.

Counters 642, 644, and 646 may each be associated with one of coordinates X, Y, or Z of cube 300 of FIG. 3A. For example, as shown in FIG. 6, counters 642, 644, and 646 may respectively be associated with coordinates Y, X, and Z. In an illustrative example, where cube 300 may be operable to store 12×12×12=1728 data samples, twelve data samples may be stored along each dimension X, Y, and Z of cube 300. Accordingly, as shown in FIG. 3B, memory locations along each dimension in cube 300 may be indexed from 0, 1, . . . , 11 and each memory location in cube 300 may be represented by coordinates (X, Y, Z), where X, Y, and Z each run from index value 0 to index value 11. Continuing this example, system 600 may be configured to compute any of equations 12(12Z+

X)+Y, 12(12X+Y)+Z, or 12(12Y+Z)+X and output the result of the computation via lead 602. The value output on lead 602 may correspond to a memory address in the buffer. Thus, system 600 may map a memory location in cube 300 to a memory address in the buffer. System 600 may be operable to generate both read and write memory addresses in the buffer in this manner.

Counters 642, 644, and 646 may be cyclic counters each operable to each output a value between 0 to 11 on respective outputs—Y of counter 642, X of counter 644, and Z of counter 646. Counters 642, 644, and 646 may all have an initial and/or default internal value of 0. Counters 642, 644, and 646 may output overflow signals O1, O2, and O3 respectively. Overflow signal O1 may be a binary valued signal that may have a logic-low value when counter 642 outputs values from 0 to 11 on output Y of counter 642. Once counter 642 outputs value 11 on output Y of counter 642, counter 642 may reset its internal counter to value 0 and simultaneously output a logic-high value for overflow signal O1. Overflow signals O2 and O3, corresponding respectively to counters 644 and 646, may exhibit similar behavior as overflow signal O1. The initial and/or default value of overflow signals O1, O2, and O3 may be a logic-low value. Counters 642, 644, and 646 may each be coupled to switch 610 and overflow signals O1, O2, and O3 may respectively be received by switch 610 as inputs x2, x3, and x4. Counters 642, 644, and 646 may receive input signals C1, C2, and C3 respectively from switch 610.

Switch 610 may be coupled to clock 612 and to each of counters 642, 644, and 646. Switch 610 may output signals u1, u2, and u3 respectively to counters 642, 644, and 646. Counters 642, 644, and 646 may receive signals u1, u2, and u3 from switch 610 respectively as inputs C1, C2, and C3. Switch 610 may be configurable to connect any of the signals it receives as inputs, i.e., clock 612, x2, x3, and x4 to any of the signals it outputs, i.e., u1, u2, and u3. For example, switch 610 may initially be configured to connect clock 612 to output u1 (transmitted to counter 642), input x2 to output u2 (transmitted to counter 644), and input x3 to output u3 (transmitted to counter 646).

Accordingly, in a first time slot in which clock 612 toggles after system 600 is powered-up, switch 610 may feed clock 612 through to counter 642 via output u1. In response to receiving the clock toggle, counter 642 may increment its internal value from 0 to 1 and output a value of 1 on output Y of counter 642. In the first time slot, the values of overflow signals O1 of counter 642 and O2 of counter 644 may be logic-low and therefore, counters 644 and 646 may receive logic-low values at respective inputs C2 and C3. Accordingly, the internal state of counters 644 and 646 may remain at 0 in the first time slot.

In subsequent time slots, switch 610 may continue to feed clock 612 to counter 642, and counter 642 may increment its internal state by a unit value in each time slot that clock 612 toggles and may output the value of the internal state on output Y of counter 642. Until the internal state of counter 642 reaches value 11, counter 642 may continue to output a logic-low value on overflow signal O1. Once the internal state of counter 642 reaches value 11, counter 642 may roll over its internal state to value 0 and toggle the value of overflow signal O1.

When switch 610 receives a toggle on input x2 from counter 642, switch 610 may feed that toggle, via output u2, to input C2 of counter 644. Accordingly, counter 644 may increment its internal state by a unit value to a value of 1 and may output the value of its internal state on output X of counter 644. The value of overflow signal O2 of counter 644 may be logic-low because the internal state of counter 644 has

not reached a value 11 yet and accordingly counter **646** may receive a logic-low value at inputs C3. The internal state of counter **646** may therefore remain at 0 in this time slot because counter **646** may not receive a toggle value on input C3.

In the next 11 time slots, switch **610** may continue to feed clock **612** to counter **642**, and counter **642** may increment its internal state by a unit value in each time slot that clock **612** toggles and may output the value of the internal state on output Y of counter **642**. During these time slots, counter **644** may output the value of its internal state, i.e., 1, on output X of counter **644**. Counter **646** may output the value of its internal state, i.e., 0, on output Z of counter **646**. When the internal state of counter **642** reaches value 11, counter **642** may roll over its internal state to value 0 and toggle the value of overflow signal O1. Accordingly, counter **644** may receive a toggle on input C2 and may accordingly increment its internal state by a unit value to a value of 2 and may output the value of its internal state on output X of counter **644**.

The process described above may be repeated such that the values output by counters **642**, **644**, and **646** respectively on outputs Y of counter **642**, output X of counter **644**, and output Z of counter **646** are as indicated below in Table 1.

TABLE 1

		Time slot									
	1	2	...	12	13	14	...	24	...	132	133	...	144
Y	0	1	...	11	0	1	...	11	...	0	1	...	11
X	0	0	...	0	1	1	...	1	...	11	11	...	11
Z	0	0	...	0	0	0	...	0	...	0	0	...	0

After the 144th time slot, when the internal state of counter **642** may have reached value 11 (as shown in TABLE 1), counter **642** may roll over its internal state to value 0 and toggle the value of overflow signal O1. Additionally, the internal state of counter **644** may have reached value 11 and counter **644** may roll over its internal state to value 0. Counter **644** may additionally toggle the value of overflow signal O2 which may be received by switch **610** at input x3.

When switch **610** receives a toggle on input x3 from counter **644**, switch **610** may feed that toggle, via output u3, to input C3 of counter **646**. Accordingly, counter **646** may increment its internal state by a unit value to a value of 1 and may output the value of its internal state on output Z of counter **646**. The process described above may be repeated such that the values output by counters **642**, **644**, and **646** respectively on outputs Y of counter **642**, output X of counter **644**, and output Z of counter **646** are as indicated below in Table 2.

TABLE 2

		Time slot							
	1	...	144	145	...	288	289	...	432	...	1728
Y	0	...	11	0	...	11	0	...	11	...	11
X	0	...	11	0	...	11	0	...	11	...	11
Z	0	...	0	1	...	1	2	...	2	...	11

The above example is merely illustrative and depicts the case where cube **300** may be operable to store 12×12×12=1728 data samples. Cube **300** may be operable to store more or less than 1728 data samples and the values of the indices in TABLES 1 and 2 may change correspondingly.

Shift registers **656** and **658** may be operable to left shift their respective inputs by 3 and 2 bits respectively. The operation of left shifting an input may be equivalent to multiplying the input, e.g., left shifting the input value by 3 bits may be equivalent to multiplying the input value by 8 and left shifting the input value by 2 bits may be equivalent to multiplying the input value by 4.

In the illustrative embodiment shown in FIG. **6**, system **600** may be configured to compute the equation 12(12Z+X)+Y. Accordingly, shift registers **656** and **658** may both receive output Z from counter **646** and shift Z by 3 bits and 2 bits respectively. Shift registers **656** and **658** may be connected to adder **630**. From shift registers **656** and **658** respectively, adder **630** may receive output Z from counter **646** that has been left shifted by 3 bits (i.e., multiplied by 8) and output Z from counter **646** that has been left shifted by 2 bits (i.e., multiplied by 4). Adder **630** may additionally receive output X from counter **644**. Adder **630** may compute 12Z+X based on the inputs it receives. Adder **630** may output the value computed for 12Z+X to shift registers **652** and **654**.

Shift registers **652** and **654** may be substantially similar to shift registers **656** and **658** respectively. Accordingly, shift registers **652** and **654** may both receive output 12Z+X from adder **630** and shift 12Z+X by 3 bits and 2 bits respectively. Shift registers **652** and **654** may be connected to adder **620**. From shift registers **652** and **654** respectively, adder **620** may receive 12Z+X left shifted by 3 bits (i.e., multiplied by 8) and 12Z+X left shifted by 2 bits (i.e., multiplied by 4). Adder **620** may additionally receive output Y from counter **642**. Adder **620** may compute 12(12Z+X)+Y based on the inputs it receives. Adder **620** may output the value computed for 12(12Z+X)+Y via lead **602**.

The above example is merely illustrative and depicts the case where system **600** is configured to compute equation 12(12Z+X)+Y. In other embodiments, system **600** may be configured to compute equations 12(12X+Y)+Z or 12(12Y+Z)+X. Switch **610** may reconfigure its internal connections dynamically when system **600** may be configured to compute equations 12(12Z+X)+Y, 12(12X+Y)+Z, or 12(12Y+Z)+X.

In some implementations, system **600** of FIG. **6** may include a state machine (not shown) operable to control the reconfiguration of switch **610**. For example, the state machine may control which of equations 12(12Z+X)+Y, 12(12X+Y)+Z, or 12(12Y+Z)+X is computed by system **600**. As discussed above in connection with FIGS. **4A**, **4B**, and **4C**, data samples may be read from or written to memory locations in cube **300** in the order Y-X-Z, X-Z-Y, or Z-Y-X. When data samples are read from or written to memory locations in cube **300** in the order Y-X-Z, system **600** may compute memory addresses in the buffer by computing equation 12(12Z+X)+Y. When data samples are read from or written to memory locations in cube **300** in the order X-Z-Y, system **600** may compute memory addresses in the buffer by computing equation 12(12Y+Z)+X. When data samples are read from or written to memory locations in cube **300** in the order Z-Y-X, system **600** may compute memory addresses in the buffer by computing equation 12(12X+Y)+Z. The state machine may control the configuration of switch **610** such that system **600** computes the equation corresponding to whether data samples are supposed to be read from or written to memory locations in cube **300** in the order Y-X-Z, X-Z-Y, or Z-Y-X.

FIG. **7** is a simplified block diagram of an addressor circuit that may be used to generate addresses for the buffer using backpressure, according to an illustrative embodiment. System **700** includes circuits **710** and **720** and comparator **730**. Each of circuits **710** and **720** may be substantially identical to system **600** described above in connection with FIG. **6**. Com-

parator **730** may be connected to circuit **710** and circuit **720** via leads **732** and **734** respectively.

In an implementation, circuit **710** may be operable to generate read addresses for the buffer while circuit **720** may be operable to generate write addresses for the buffer.

In this manner, data samples may be read from and written to different memory addresses in the buffer simultaneously. The simultaneous reading from and writing to of data samples in the buffer may proceed in the manner described above in connection with FIGS. **4A**, **4B**, and **4C**.

Comparator **730** may be operable to generate a binary valued backpressure signal operable to ensure that read memory addresses generated by circuit **710** do not overlap with write memory addresses generated by circuit **720**. Comparator **730** may output the backpressure signal on lead **740** which may be connected to circuit **720** as shown in FIG. **7**. Lead **740** may be connected to a clock operable to supply a clock signal to circuit **720**. The backpressure signal may equivalently be a clock enable signal, i.e., when the backpressure signal has a logic-high value the clock of circuit **720** may be activated and when the backpressure signal has a logic-low value the clock of circuit **720** may be disabled. When the clock of circuit **720** is disabled, computations of circuit **720** may temporarily be paused. In this way, if comparator **730** determines that the write address is in conflict with the read address (e.g., the write address is ahead of the read address or the write address is a memory location from which data has not yet been read) then the logic-low value backpressure signal may prevent circuit **720** from generating additional write addresses. If comparator **730** determines that the write address is not in conflict with the read address, comparator **730** may generate a logic-high backpressure signal activating the clock of circuit **720**.

Comparator **730** may be operable to generate the backpressure signal by comparing the memory read address received from circuit **710** via lead **732** to the memory write address received from circuit **720** via lead **734**. Based on the read address, comparator **730** may determine whether the memory slice of cube **300** which contains the received memory address has been released, i.e., data samples have already been read from it. As described above in connection with FIGS. **4A**, **4B**, and **4C**, if a memory slice has been released, that memory slice is then free to have other data samples written to it.

FIG. **8** illustrates a circuit or other device that includes embodiments of the delay determination circuits described herein as being within a data processing system **800**. In an embodiment, the circuit or device may be an integrated circuit, application specific standard product (ASSP), application specific integrated circuit (ASIC), programmable logic device (PLD), full-custom chip, or dedicated chip. In an embodiment, circuit **860** may be substantially similar to circuit **100**. Data processing system **800** can include one or more of the following components: a processor **870**, memory **880**, I/O circuitry **880**, and peripheral devices **840**. These components are connected together by a system bus or other interconnections **830** and are populated on a circuit board **820** which is contained in an end-user system **810**.

System **800** could be used in a wide variety of applications, such as computer networking, data networking, instrumentation, video processing, digital signal processing, or any other application where the advantage of using programmable or reprogrammable logic is desirable. Circuit **860** can be used to perform a variety of different logic functions. For example, circuit **860** can be configured as a processor or controller that works in cooperation with processor **870**. Circuit **860** may also be used as an arbiter for arbitrating access to a shared resource in system **800**. In yet another example, circuit **860** can be configured as an interface between processor **870** and one of the other components in system **800**. It should be noted that system **800** is only exemplary, and that the true scope and spirit of the invention should be indicated by the following claims.

Although components in the above disclosure are described as being connected with one another, they may instead be connected to one another, possibly via other components in between them. It will be understood that the foregoing are only illustrative of the principles of the invention, and that various modifications can be made by those skilled in the art without departing from the scope and spirit of the invention. One skilled in the art will appreciate that the present invention can be practiced by other than the described embodiments, which are presented for purposes of illustration and not of limitation, and the present invention is limited only by the claims that follow.

What is claimed is:

1. A system for mapping memory locations of a 3D memory to a buffer, the system comprising circuitry for:
   determining a first geometric pattern for storing data in the 3D memory based on a type of computation performed using the data as input;
   storing the data in the 3D memory using the determined first geometric pattern;
   mapping memory locations arranged in the first geometric pattern in the 3D memory to first memory locations in the buffer;
   writing data to the first memory locations in the buffer;
   mapping memory locations arranged in a second geometric pattern in the 3D memory to second memory locations in the buffer, wherein the memory locations in the second geometric pattern in the 3D memory overlap with the memory locations in the first geometric pattern in the 3D memory;
   reading data from the second memory locations in the buffer after writing data to the first memory locations in the buffer; and
   writing data to the second memory locations in the buffer after reading data from the second memory locations in the buffer.

2. The system of claim **1**, wherein the circuitry is further operative to:
   map memory locations arranged in a third geometric pattern in the 3D memory to third memory locations in the buffer, wherein the memory locations in the third geometric pattern in the 3D memory overlap with the memory locations in the second geometric pattern in the 3D memory;
   read data from the third memory locations in the buffer;
   write data to the third memory locations in the buffer after reading data from the third memory locations in the buffer; and
   read data from the first memory locations in the buffer after writing data to the third memory locations in the buffer.

3. The system of claim **2**, wherein the:
   3D memory is a symmetric cube;
   first geometric pattern is a slice of the 3D memory along a first dimension of the symmetric cube;
   second geometric pattern is a slice of the 3D memory along a second dimension of the symmetric cube; and
   third geometric pattern is a slice of the 3D memory along a third dimension of the symmetric cube.

4. The system of claim **1**, wherein mapping memory locations arranged in the first geometric pattern in the 3D memory further comprises generating memory addresses associated

with the first memory locations in the buffer based on corresponding memory locations arranged in the first geometric pattern in the 3D memory.

5. The system of claim 1, wherein the first memory locations in the buffer and the second memory locations in the buffer are locked.

6. The system of claim 1, wherein the second memory locations in the buffer are released in response to reading data from the second memory locations in the buffer.

7. The system of claim 2, wherein the size of the symmetric cube is selected to store a number of data samples substantially corresponding to a size of a largest data frame.

8. The system of claim 1, wherein the circuitry is further configured to generate a backpressure enable signal to control a rate at which data is streamed to the buffer.

9. A method for mapping memory locations of a 3D memory to a buffer, the method comprising:

determining a first geometric pattern for storing data in the 3D memory based on a type of computation performed using the data as input;

storing the data in the 3D memory using the determined first geometric pattern;

mapping memory locations arranged in the first geometric pattern in the 3D memory to first memory locations in the buffer;

writing data to the first memory locations in the buffer;

mapping memory locations arranged in a second geometric pattern in the 3D memory to second memory locations in the buffer, wherein the memory locations in the second geometric pattern in the 3D memory overlap with the memory locations in the first geometric pattern in the 3D memory;

reading data from the second memory locations in the buffer after writing data to the first memory locations in the buffer; and

writing data to the second memory locations in the buffer after reading data from the second memory locations in the buffer.

10. The method of claim 9 further comprising:

mapping memory locations arranged in a third geometric pattern in the 3D memory to third memory locations in the buffer, wherein the memory locations in the third geometric pattern in the 3D memory overlap with the memory locations in the second geometric pattern in the 3D memory;

reading data from the third memory locations in the buffer;

writing data to the third memory locations in the buffer after reading data from the third memory locations in the buffer; and

reading data from the first memory locations in the buffer after writing data to the third memory locations in the buffer.

11. The method of claim 10, wherein the:

3D memory is a symmetric cube;

first geometric pattern is a slice of the 3D memory along a first dimension of the symmetric cube;

second geometric pattern is a slice of the 3D memory along a second dimension of the symmetric cube; and

third geometric pattern is a slice of the 3D memory along a third dimension of the symmetric cube.

12. The method of claim 9, wherein mapping memory locations arranged in the first geometric pattern in the 3D memory further comprises generating memory addresses associated with the first memory locations in the buffer based on corresponding memory locations arranged in the first geometric pattern in the 3D memory.

13. The method of claim 9, wherein the first memory locations in the buffer and the second memory locations in the buffer are locked.

14. The method of claim 9, wherein the second memory locations in the buffer are released in response to reading data from the second memory locations in the buffer.

15. The method of claim 10, wherein the size of the symmetric cube is selected to store a number of data samples substantially corresponding to a size of a largest data frame.

16. The method of claim 9 further comprising generating a backpressure enable signal to control a rate at which data is streamed to the buffer.

17. A system for generating addresses based on 3D memory for a buffer, the system comprising circuitry for:

determining a first geometric pattern for storing data in the 3D memory based on a type of computation performed using the data as input;

storing the data in the 3D memory using the determined first geometric pattern;

mapping memory locations arranged in a first geometric pattern in the 3D memory to first memory locations in the buffer;

generating memory addresses associated with the first memory locations in the buffer based on corresponding memory locations arranged in the first geometric pattern in the 3D memory;

writing data to the first memory locations in the buffer;

mapping memory locations arranged in a second geometric pattern in the 3D memory to second memory locations in the buffer;

generating memory addresses associated with the second memory locations in the buffer based on corresponding memory locations arranged in the second geometric pattern in the 3D memory; and

reading data from the second memory locations in the buffer after writing data to the first memory locations in the buffer.

18. The system of claim 17, wherein the first memory locations in the buffer and the second memory locations in the buffer are locked.

19. The system of claim 18, wherein the second memory locations in the buffer are released in response to reading data from the second memory locations in the buffer.

20. The system of claim 17, wherein the circuitry is further configured to generate a backpressure enable signal to control a rate at which data is streamed to the buffer.

* * * * *